

la solution de (4) est

$$a_n = \int_0^{\tau} \frac{d\tau}{\sin^2 h_n \tau} \int_0^{\tau} Y_n e^{w\tau} \sin \tau d\tau$$

par conséquent u :

$$u = \sum_{n=1}^{n=\infty} \sin k_n x \left[\int_0^{\tau} \frac{d\tau}{\sin^2 h_n \tau} \int_0^{\tau} Y_n e^{w\tau} \sin h_n \tau \right] \sin h_n \tau \quad (5)$$

Cette expression peut être réduite à:

$$u(x_1, \tau_1) = \sum_{n=1}^{n=\infty} \frac{\sin k_n x_1}{h_n} \int_0^{\tau_1} \sin h_n (\tau_1 - \tau) Y_n e^{w\tau} d\tau.$$

La solution donnée ici satisfait aux conditions au bord ordinaires.

Mathematics. — MONNA, A. F.: *On a linear P-adic space*, p. 74.

Be ℓ_p^p ($p \geq 1$) the space whose elements are the ranges (x_1, x_2, \dots) of P -adic numbers such that $\sum_i |x_i|_p^p$ converges. The norm of x is defined by

$$\|x\| = \left\{ \sum_i |x_i|_p^p \right\}^{\frac{1}{p}}.$$

The strong convergence is defined in the usual way. The space is complete (P -adic BANACH-space) and separable. We have

$$\|x + y\| \leq \|x\| + \|y\|; \|x + y\| \leq \max(\|x\|, \|y\|)$$

is not true in general. The notions "operator" and "functional" are defined in the usual way. A necessary and sufficient condition for the linearity of an additive operator is given:

$$\|U(x)\| \leq M P^k \text{ for } \|x\| \leq P^k.$$

The general form of the linear functionals is given by ${}^P \sum C_i x_i$, where $\{|C_i|_p\}$ is a bounded range; this is valuable for $p \geq 1$. For the P -adic convergence of this series for all x in ℓ_p^p , it is a necessary and sufficient condition that $\{|C_i|_p\}$ is bounded.

The weak convergence is introduced as usual by the linear functionals. It is probable that the strong and the weak convergence are identical. This is shown for $p > 1$ in the case that the given range $\{x^{(n)}\}$ weak convergent to $x = \{x_i\}$, satisfies the condition that in the ranges $\{|x_i^{(n)} - x_i|_p\}$ all terms $\neq 0$ are different.

Finally the weak convergence of the functionals and the orthogonality of the vectors is studied.