

## ASTRONOMY

# THE VALUE OF OBSERVATIONS OF CONTINUOUS SPECTRA IN THE CHROMOSPHERE AND PROMINENCES

BY

H. ZANSTRA

*(Circular No 1 of the Astronomical Institute of the University of Amsterdam)*

(Communicated at the meeting of Sept. 30, 1950)

### *Summary*

The intensity of the continuous spectrum for various wavelengths to be expected in the chromosphere and in prominences is computed for electron temperatures of  $5000^\circ$ ,  $10,000^\circ$ ,  $20,000^\circ$  and  $30,000^\circ$  and electron or proton concentrations of the order  $10^{11}$  (chromosphere) and  $10^{10}$  (prominences). The result contained in Figures 2 to 5 and Table 2 may serve as a guide for future eclipse observations. It is pointed out that present evidence points to a chromospheric electron temperature a good deal lower than REDMAN's kinetic temperature of about  $30,000^\circ$  for atoms and ions. The spectra considered are the  $Ba_c$  spectrum, the other recombination and electron switch spectra indicated by  $C$  and that by scattering of photospheric light by free electrons marked  $c$ . For the chromosphere the determination of electron or proton concentration as well as of electron temperature appears possible. For prominences one can determine concentration and thickness, provided the electron temperature be known. A remark concerning the possible influence of the continuous spectrum due to the formation of negative hydrogen ions is made.

### 1. *Introduction* \*)

Continuous spectra in the chromosphere and in prominences have been treated by various investigators. DAVIDSON, MINNAERT, ORNSTEIN and STRATTON, <sup>1)</sup> carried out approximate measurements of relative intensity for slit spectra taken by DAVIDSON and STRATTON at the 1926 eclipse. The continuous spectrum at the head of the BALMER series indicated electron temperature of  $3600^\circ$  for the lower chromosphere,  $4000^\circ$  for a prominence in the flash spectrum and  $3200^\circ$  for a prominence in the coronal spectrum. For the high prominence, the relative distribution in the region  $\lambda$  4100 to 3800 was equivalent to a black body temperature

---

\*) The considerations set forth in the present paper were presented in an abbreviated form at the Astronomical Colloquium "Problems on Solar Physics" arranged in Dublin by Dunsink Observatory, September 21, 1950.

<sup>1)</sup> C. R. DAVIDSON, M. MINNAERT, L. S. ORNSTEIN and J. F. M. STRATTON, M.N. 87, 536 (1928).

of about  $2000^\circ$ . CILLIÉ and MENZEL <sup>2)</sup>, discussing slitless spectrograms taken by CHAPPEL and MENZEL at the 1932 eclipse, found a chromospheric electron temperature of about  $10,000^\circ$  from the relative distribution of the  $Ba_c$  spectrum. The absolute intensity of the  $Ba_c$  spectrum yielded an electron or proton concentration of  $3.8 \times 10^{11}$  per  $\text{cm}^3$  at the base of the chromosphere, likewise from KRAMERS' theory. This agrees, as regards order of magnitude, with PANNEKOEK's <sup>3)</sup> value of  $6 \times 10^{11}$  from the overlapping of the higher lines of the BALMER series due to STARK effect <sup>3)</sup>. For prominences observed with the coronagraph LYOT <sup>4)</sup> found for the continuous spectrum in the region  $\lambda$  5950 to 6400 a degree of polarisation of about 15 per cent, after correction for atmospheric scattering, and concludes that it is mainly produced by scattering of photospheric light by the free electrons in the prominence. On the basis of this assumption, WURM <sup>5)</sup> has recently shown that the ratio of the intensity of the  $Ba_c$  spectrum to the continuous spectrum at longer wavelength gives a method for determining the proton or electron concentration per  $\text{cm}^3$  for a prominence, if the electron temperature be known, and carried out an approximate estimate on this basis.

The foregoing clearly shows the importance of observations of intensities of the continuous spectrum at various wavelengths in the chromosphere and prominences, preferably from spectra taken during an eclipse.

Thus far the  $Ba_c$  spectrum and the scattering from free electrons, which will be indicated by the suffix *c*, has received most of the attention. For a complete discussion however, also the other recombination spectra due to captures on levels higher than the second plus the electron switch spectra must be considered and will in total be indicated by a capital *C*. The intensity of this *C* spectrum, like that of the  $Ba_c$  spectrum, follows from the KRAMERS theory. In the following the intensities of these three kinds of spectra to be expected theoretically will be worked out for a few electron temperatures and concentrations, to serve as a future guide for eclipse observations. Also a few provisional conclusions of a very approximate nature will be drawn. The results of the KRAMERS theory, which are given, might be slightly modified by the quantum mechanics, which can be done eventually by the use of GAUNT factors. Another source of continuous spectra might be furnished by captures of free electrons by neutral hydrogen atoms and corresponding electron switches. This will briefly be considered at the end of the paper, but is not thought to be of much importance for the matter on hand.

## 2. *Intensities of the various continuous spectra to be expected*

In the following it will generally be assumed that most of the electrons

<sup>2)</sup> G. G. CILLIÉ and D. H. MENZEL, Harvard Circular, no. 410 (1935).

<sup>3)</sup> A. PANNEKOEK, M.N. 98, 694 (1938).

<sup>4)</sup> B. LYOT, Comptes Rendus 202, 392 (1936).

<sup>5)</sup> K. WURM, Mitt. Hamb. Sternw. Bergedorf 21, 103 (1948), no. 206.

originate from hydrogen atoms and only very few form negative hydrogen, so that the concentration per cm<sup>3</sup> of electrons  $n_e$  becomes equal to that of protons  $n_1$ . Moreover the electron temperature  $T_e$  is considered not to vary throughout the chromosphere or the prominence.

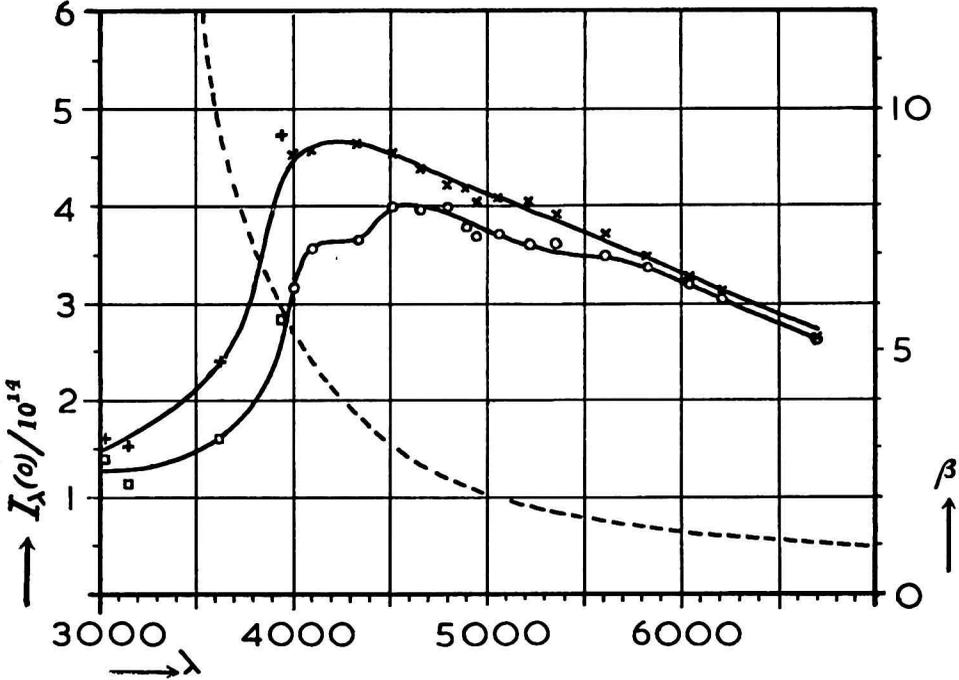


Fig. 1. Values of the intensity at the centre of the sun's disc according to MULDER'S. Upper drawn curve:  ${}_0I_\lambda(0)$  for the continuous background. Lower drawn curve:  ${}_0I_\lambda(0)$  for the spectrum with the FRAUNHOFER lines fuzzed out. Crosses and circles refer to H. H. PLASKETT'S observations, vertical crosses and squares to those of FABRY. The dotted curve and righthand scale give the darkening coefficient.

Let  $\varepsilon_\lambda d\lambda$  be the energy of one of the continuous spectra emitted in a certain direction per unit solid angle per second per cm<sup>3</sup>, and  $E_\lambda d\lambda$  the same quantity per cm<sup>2</sup>, or intensity per cm<sup>2</sup> which is observed or predicted. Then

$$(1) \quad E_\lambda = \int \varepsilon_\lambda dl$$

where  $dl$  is the element of length along the line of sight.

According to KRAMERS' theory as worked out by CILLIÉ<sup>6)</sup>, the emission per cm<sup>3</sup> per second per unit frequency for hydrogen is given by

$$(2) \quad J_n(\nu) d\nu = n_1 n_e \frac{Q}{n^3 T_\varepsilon^{3/2}} e^{-\frac{h\nu - x_n}{kT_\varepsilon}} d\nu,$$

$$(2a) \quad J'_n(\nu) d\nu = n_1 n_e \frac{Q'}{T_\varepsilon^{1/2}} e^{-\frac{h\nu}{kT_\varepsilon}} d\nu,$$

where  $J_n$  refers to captures on the level  $n$  and  $J'$  to electron switches.

<sup>6)</sup> G. G. CILLIÉ, M.N. 92, 820 (1932) and 96, 771 (1936).

The constants in the present paper are based on BIRGE's 1941 values <sup>7)</sup>, which give

$$(2b) \quad Q = (2.170 \pm 0.005) \times 10^{-32}, \quad Q' = (6.88 \pm 0.01) \times 10^{-38}.$$

It may be remarked that for objects outside the sun's limb only spontaneous captures should be considered. Forced captures, being negative absorptions, only come into play when the object is observed projected on the disc, strengthening the incident beam without altering its direction.

To obtain  $\varepsilon_\lambda$  from  $J_n$  or  $J'$  one has to multiply by  $c/(4\pi\lambda^2)$ . Equations (2) and (2a) readily yield the intensity  $E_{Ba_c}$  of the  $Ba_c$  spectrum at the series limit and of the other spectra added together  $E_{\lambda C}$  and their ratio

$$(3) \quad \frac{E_{\lambda C}}{E_{Ba_c}} = \frac{\varepsilon_{\lambda C}}{\varepsilon_{Ba_c}}$$

since  $T_e$  was considered constant. These values for four electron temperatures are plotted in Figures 2, 3, 4 and 5 using the result of BARBIER's <sup>8)</sup> computations, slightly extended, in the full-drawn curves marked with a capital  $C$ . Likewise the ratio  $E_{\lambda Ba_c}/E_{Ba_c}$  of the intensity of the  $Ba_c$  spectrum at the wavelength  $\lambda$  to its value at the series head is represented by the full-drawn curve marked  $Ba_c$ .

For  $n = 2$ , equation (2) yields at the series limit  $\lambda$  3646.9

$$(4) \quad \varepsilon_{Ba_c} \equiv \varepsilon_{3646 Ba_c} = (4.86 \pm 0.01) \times 10^{-21} n_1 n_e \left(\frac{10^4}{T_e}\right)^{3/2}.$$

For scattering of photospheric light by free electrons just above the photosphere, the  $c$  spectrum, one has

$$(5) \quad \varepsilon_{\lambda c} = I_\lambda(0) \frac{\frac{1}{2} + \frac{15}{64} \beta}{1 + \beta} \sigma n_e$$

where  $\sigma$  the scattering coefficient per electron

$$(5a) \quad \sigma = (6.67 \pm 0.01) \times 10^{-25}.$$

In this formula  $I_\lambda(0)$  represents the intensity at the centre of the solar disc and  $\beta$  the coefficient of darkening for the wave length  $\lambda$ . It may be obtained from equations (3), (4) and (5) of a former paper by the writer <sup>9)</sup> for scattering by an oscillator, which applies equally well to the present case.

The values of  $I_\lambda(0)$  were taken from MULDER'S, <sup>10)</sup> essentially using a re-plot of his Fig. 2, from his Tables VI and VII. It is represented in our

<sup>7)</sup> R. T. BIRGE, Reports on Progress in Physics of the Physical Society 8, 90 (1941).

<sup>8)</sup> D. BARBIER, Ann. d'Astrophys. 7, 80 (1944). His  $J'$  for 30,000° (p. 104) should be 0.0255.

<sup>9)</sup> H. ZANSTRA, M.N. 101, 250 (1941).

<sup>10)</sup> G. F. H. MULDER'S, Aequivalente breedten van FRAUNHOFER-lijnen in het zonnenspectrum. Proefschrift Utrecht (1934).

Fig. 1. The upper curve represents  ${}_0I_\lambda(0)$ , the intensity of the continuous background, which he has obtained by correcting for absorption lines, the lower curve his  $I_{red}$  representing the spectrum in which all lines are fuzzed out except the very strongest of ROWLAND intensity larger than 20. We may take  $I_{red}$  equal to our  $I_\lambda(0)$ , since scattering by free electrons will result in a fuzzing out on account of the small mass and consequent high thermal velocity. The values of  $\beta$  were obtained from a re-plot of MINNAERT'S <sup>11)</sup> values of  $I_\lambda(0)/F_\lambda$  based on ABBOT'S observations using the expression

$$\frac{F_\lambda}{I_\lambda(0)} = \frac{1 + \frac{2}{3}\beta}{1 + \beta}$$

as a definition of  $\beta$ , so that this  $\beta$  gives the correct flux. The values of  $\beta$  are given by the dotted curve in Fig. 1, using the right hand scale, or, more accurately by Table 1.

TABLE I

$\lambda$	3500	3646	4000	4500	5000	5500	6000	6500	7000
$\beta$	14.1	9.6	5.36	3.05	2.05	1.56	1.26	1.06	0.93

From equations (1), (4), (5) and (5a) follows the expression for the ratio of intensity per cm<sup>2</sup> of the scattering spectrum  $c$  at wave length  $\lambda$  to the  $Ba_c$  spectrum at  $\lambda$  3646

$$(6) \quad \frac{E_{\lambda c}}{E_{Ba_c}} = (0.684 \pm 0.001) \frac{1 + \frac{15}{32}\beta}{1 + \beta} \cdot \frac{I_\lambda(0)}{10^{14}} \cdot \left(\frac{T_e}{10^4}\right)^{3/2} \cdot \frac{10^{10}}{\bar{n}_1},$$

where

$$(6a) \quad \bar{n}_1 = \frac{\int n_1 n_e dl}{\int n_e dl}.$$

The quantity  $\bar{n}_1$  may be termed the effective concentration of protons for the ratio of  $c$  to  $Ba_c$  intensity. Equation (6) enables to determine  $\bar{n}_1/T_e^{3/2}$  from the observed intensity ratio  $E_{\lambda c}/E_{Ba_c}$ , which is WURM'S method. It is however somewhat more refined than the equation given by WURM, since the dependence of scattering upon direction is taken into account and central intensity with darkening coefficient has been used in preference to the black body approximation.

If, as an approximation, the object is assumed to have a thickness  $L$  within which the concentration  $n_1$  or  $n_e$  is constant, (1) and (6a) reduce to

$$E_\lambda = \varepsilon_\lambda L, \quad (1a) \quad \bar{n}_1 = n_1 = n_e. \quad (6b)$$

One might assume this for prominences.

For the chromosphere however one may, following CILLIÉ and MENZEL, assume a concentration  $n_1$  or  $n_e$  falling off with height  $x$  as  $e^{-\lambda a' x}$ , where  $x$  is very much smaller than the solar radius. Then (6a) leads to

$$(7) \quad \bar{n}_1 = \frac{n_1(x)}{\sqrt{2}} = \frac{n_e(x)}{\sqrt{2}},$$

<sup>11)</sup> M. MINNAERT, B.A.N. 2, 75 (1942), no. 51, Table IV and Fig. 3.

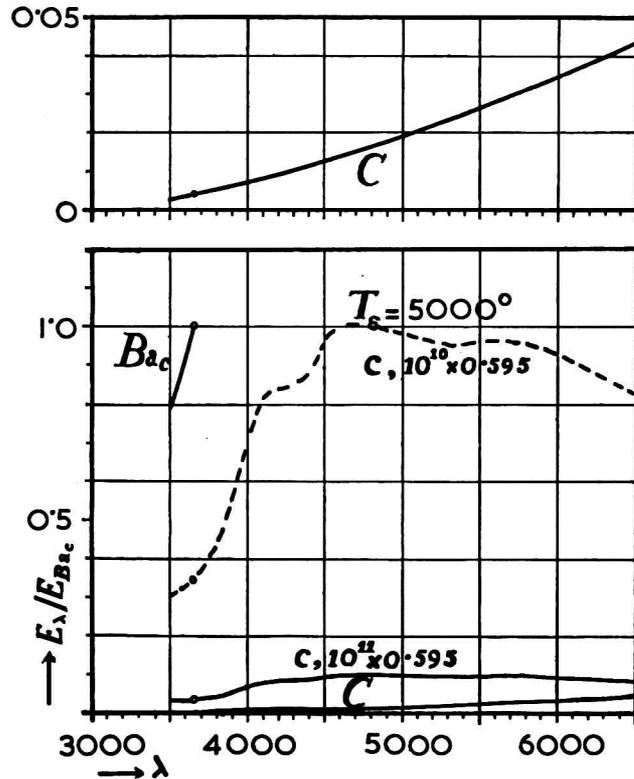


Fig. 2. Theoretical intensities of continuous spectra, expressed in the  $Ba_c$  intensity at the head as a unit:  $C$  for all recombination and electron switch spectra except  $Ba_c$ ;  $c$  for scattering of photospheric light by free electrons, followed by the effective concentration of protons or electrons. The full drawn  $c$  curve is typical for the chromosphere at 1300 km, and the dotted curve for a prominence. Electron temperature  $5000^\circ$ .

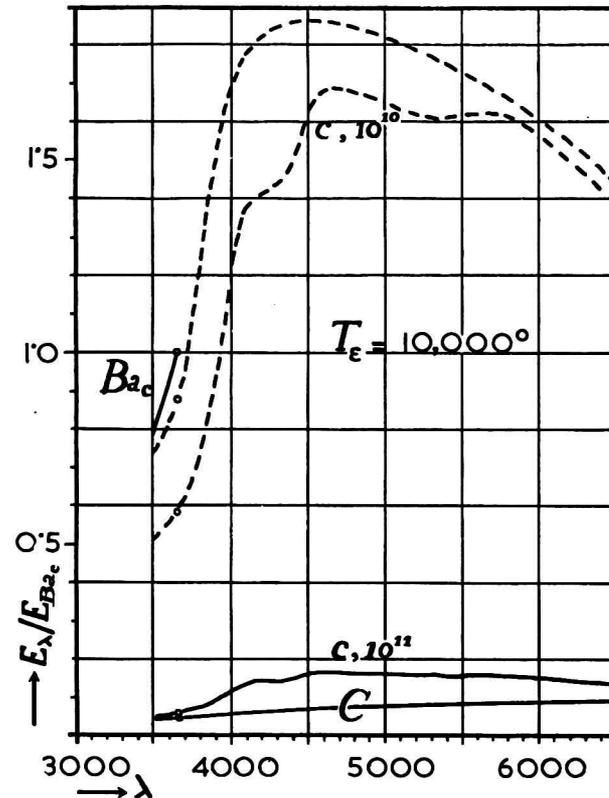


Fig. 3. The same as Fig. 2, but for electron temperature  $10,000^\circ$ . The upper dotted curve refers to scattering without FRAUNHOFER lines. N.B. The value of  $E_{\lambda c}/E_{Ba_c}$  for any  $\bar{n}_1$ , and any  $T_e$ , is obtained by multiplying the reading of the lower dotted curve by  $\frac{T_e}{10^4} \cdot \frac{10^{10}}{\bar{n}_1}$ .

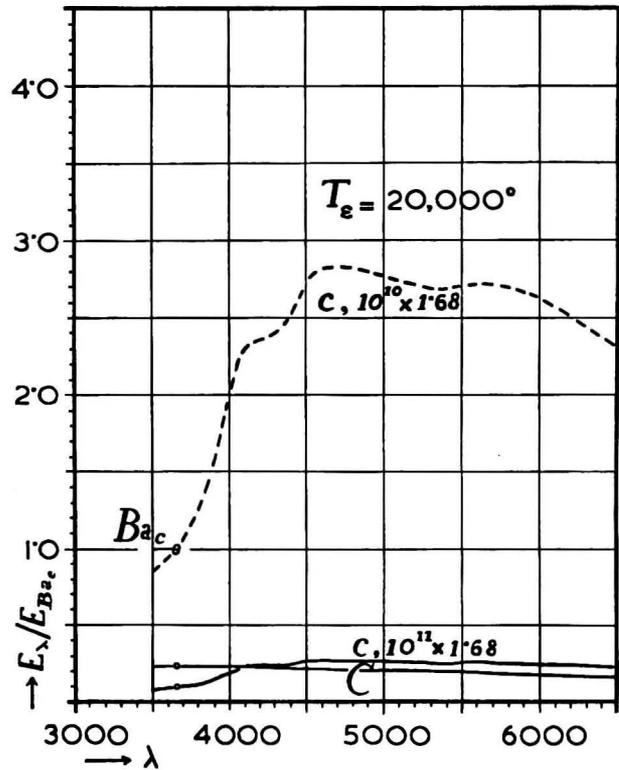


Fig. 4. The same as Fig. 2, but for electron temperature 20,000°.

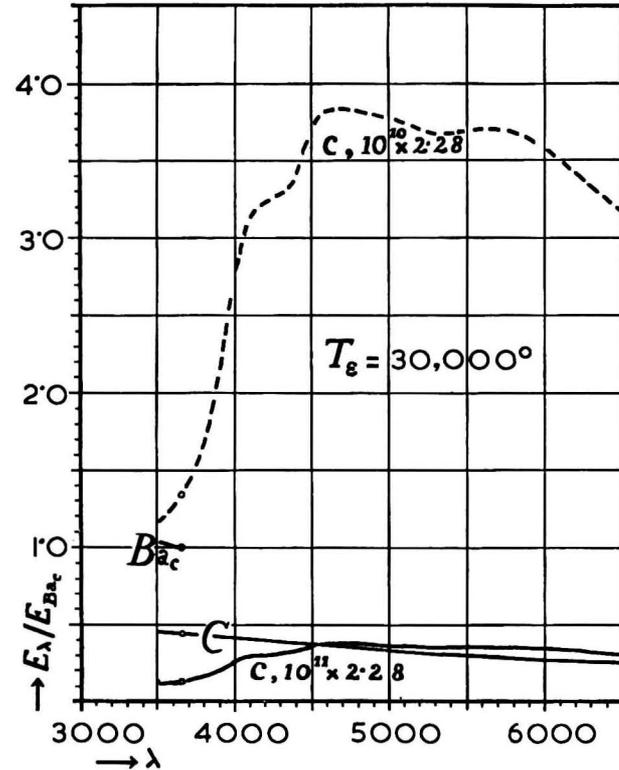


Fig. 5. The same as Fig. 2, but for electron temperature 30,000°.

if  $x$  represents the height at which the line of sight approaches closest to the limb.

From their observed absolute values of the intensity of the  $Ba_c$  spectrum and KRAMERS' theory then follows

$$(8) \quad E_{Ba_c} = 3.62 \times 10^{12} e^{-a'x}, \quad n_e(x) = n_1(x) = 3.8 \times 10^{11} e^{-1/2 a'x} \left(\frac{T_e}{10^4}\right)^{3/4},$$

C.&M.

where  $a' = 1.54 \times 10^{-3} \text{ km}^{-1}$ . For  $x = 1300 \text{ km}$  one gets

$$\bar{n}_1 = n_1(x)/\sqrt{2} = 10^{11} \left(\frac{T_e}{10^4}\right)^3.$$

In Figures 2, 3, 4 and 5 the values of  $E_{\lambda c}/E_{Ba_c}$  from (6), using  $I_\lambda(0)$  and  $\beta$  from Fig. 1, are plotted against  $\lambda$  for four different electron temperatures and these values of  $\bar{n}_1$  corresponding to a chromospheric height of 1300 km. The curves are full-drawn and marked with a  $C$ , followed by this value of  $\bar{n}_1$ . They are meant as a guide for future eclipse observations to estimate the intensity of the scattering spectrum  $c$  to be expected. Its estimated absolute value follows by multiplication by CILLIÉ and MENZEL's value of  $E_{Ba_c}$  given in (8) and can be compared with the continuous background  ${}_0I_\lambda(0)$  for the centre of the sun by means of Fig. 1. Once the new eclipse observations are carried out, the values (8) for  $E_{Ba_c}$  and  $n_1(x)$  viz  $\bar{n}_1(x)$  should of course be replaced by new values following from these observations. The value  $E_{\lambda c}/E_{Ba_c}$  for the KRAMERS spectrum  $C$  is given by the curves marked  $C$  and is determined by the electron temperature only, independent of the concentration.

### 3. Provisional Conclusions for the Chromosphere

For wavelengths longer than the series limit  $\lambda 3646.9$  one should take the sum  $E_{\lambda c} + E_{\lambda c}$ , and for shorter wavelengths the sum  $E_{\lambda Ba_c} + E_{\lambda c} + E_{\lambda c}$ . This is done in Table II for the wavelengths  $\lambda 5000$ ,  $\lambda 3700$  and  $\lambda 3647$  just adjoining  $Ba_c$ , as compared with  $\lambda 3646 Ba_c$ . The values in parentheses are the same with the  $c$  spectrum left out.

TABLE II

*Chromosphere = 1300 km. Values of  $E_\lambda/E_{3646}$  expected for three  $\lambda$ 's.*

The values in parentheses are those for  $E_{\lambda c} \rightarrow 0$  or  $\bar{n}_1 \rightarrow \infty$  and should provide lower limits for any concentration or any height

$T_e$	5000°	10,000°	20,000°	30,000°
$\frac{E_{5000}}{E_{3646}}$	0.113	0.219	0.33	0.45
	(0.0191)	(0.073)	(0.170)	(0.236)
$\frac{E_{3700}}{E_{3646}}$	0.040	0.104	0.254	0.374
	(0.0046)	(0.0049)	(0.187)	(0.308)
$\frac{E_{3647}}{E_{3646}}$	0.038	0.098	0.248	0.369
	(0.0042)	(0.0047)	(0.187)	(0.312)

Examining the reproduction of the chromospheric slit spectrum taken

at the 1926 eclipse by DAVIDSON and STRATTON<sup>12)</sup>, one cannot escape the impression that at  $\lambda$  3700 the continuous spectrum, which hardly registers there, is extremely weak as compared with  $\lambda$  3646, and that the ratio falls considerably below the value 0.37 or 0.31 of the Table required for  $T_e = 30,000^\circ$ . This would mean that the electron temperature of the chromosphere falls a good deal below the kinetic temperature of about  $30,000^\circ$  for atoms and ions, which REDMAN<sup>13)</sup> derived from line widths at the 1940 eclipse. Theorists<sup>14)</sup> thus far have mostly been assuming that the two kinetic temperatures of electrons and atoms or ions have the same value of about  $30,000^\circ$ , and for this reason chromospheric observations actually determining the electron temperature would be of great theoretical importance. A much lower electron temperature than  $30,000^\circ$  might perhaps be explained by the electrons losing their thermal energies by exciting collisions, as is the case in nebulae.

For future eclipse observations the best procedure would probably be to determine  $n_1$  by PANNEKOEK's method from the STARK broadening of the higher BALMER lines, preferably by measuring line profiles corrected for instrumental profile, thermal velocities and fine structure. This gives a kind of average  $n_1$ , which could serve for  $\bar{n}_1$ . Assuming STARK effect due to protons only with  $\bar{n}_1 = 10^{11}$ , one expects for quantum number  $n = 25$  a STARK width of about one quarter of the kinetic theory width at  $30,000^\circ$ , while the separation between subsequent lines is four times this kinetic theory width. For  $n = 30$ , the figures are 1/3 and 2.4. So it appears possible to measure the STARK effect in the wings, since its intensity falls off less rapidly with the distance from the line centre than for the kinetic theory profile.

The ratio  $E_\lambda/E_{3646}$  should further be measured, which for a given  $\lambda$  is a known function of  $\bar{n}_1$  and  $T_e$ , and  $\bar{n}_1$  being known,  $T_e$  would be determined.<sup>15)</sup> Independent determinations for various  $\lambda$  might provide a check. Provided the observed continuum between lines is strong enough in the ultraviolet, one might find it possible to extrapolate from longer wave lengths to  $\lambda$  3647 (see the last row in Table II) which would eliminate the effect of differential absorption in the ultraviolet.

If the STARK effect method does not give satisfactory results, it might be replaced or checked by the absolute determination of  $E_{Ba_c}$  which yields  $n_1/T_e^{3/4}$  according to KRAMERS' theory. (Cf. equation (8)). However

<sup>12)</sup> C. R. DAVIDSON and F. J. M. STRATTON, *Memoirs of the R.A.S.* **64**, 105 (1927), Plate 1, DAVIDSON, MINNAERT, ORNSTEIN and STRATTON, loc. cit., Plate 7.

<sup>13)</sup> R. O. REDMAN, *M.N.* **102**, 140 (1942).

<sup>14)</sup> Cf. R. N. THOMAS, *Ap. J.* **108**, 142 (1948); R. G. GIOVANELLI, *M.N.* **109**, 298 (1949).

<sup>15)</sup>  $E_{\lambda c}/E_{Ba_c}$  (3), (2), (2a) is known as  $f(T_e)$ .

$E_{\lambda c}/E_{Ba_c}$  (6) is a known constant times  $T_e^{3/2}/\bar{n}_1$ . The extreme case  $\bar{n}_1 = \infty$ ,  $E_{\lambda c} = 0$  gives therefore  $T_e$  directly. The other extreme  $E_{\lambda c} = 0$  gives  $T_e^{3/2}/\bar{n}_1$  or  $T_e$  for known  $\bar{n}_1$ . There should be no difficulty for the general case.

if the chromosphere has a filamentary structure, this method of CILLIÉ and MENZEL should give low values, since it would give a kind of average concentration, while PANNEKOEK's and WURM's methods would refer to the concentration in the filaments.

One might also think of determining  $T_e$  from the relative distribution in wave length in the  $Ba_c$  spectrum from KRAMERS' Theory with GAUNT factors, but the results thus far obtained for the chromosphere and the experience of the same method with nebulae seems to show that this method is not very reliable.

It would be very desirable to have the investigation of the continuous spectra leading to an electron temperature carried out at the same eclipse where the kinetic temperature from line widths is determined, if possible at the same spot in the chromosphere, so as to make sure that the two temperatures are determined under the same circumstances.

#### 4. Prominences

Individual concentrations in prominences may vary a great deal from case to case. The average derived by UNSÖLD<sup>16)</sup> is  $n_e = n_1 = 8 \times 10^9$ . Let us assume, merely for the purpose of illustration, a concentration  $n_1$  in prominences of one tenth of the  $n_1$  values we took as typical for chromosphere. Then, by the procedure outlined in section 2, the dotted curves of Figures 2, 3, 4 and 5 are obtained for the ratio  $E_{\lambda c}/E_{Ba_c}$  in prominences, which are marked by  $c$ , followed by the value of  $n_1$ . For the other ratios  $E_{\lambda C}/E_{Ba_c}$  and  $E_{\lambda Ba_c}/E_{Ba_c}$  the full-drawn curves remain valid. Figure 3 applies to  $T_e = 10,000^\circ$ ,  $n_1 = 10^{10}$  protons or electrons per  $\text{cm}^3$  and contains also the curve for scattering by free electrons if the solar spectrum would be free from FRAUNHOFER lines, that is if  $I_\lambda(0)$  of Fig. 1 would be replaced by  ${}_0I_\lambda(0)$ .

Figures 2 to 5 show that probably always  $E_{\lambda c}$  is much larger than  $E_{\lambda C}$ , so that scattering by free electrons predominates for wavelengths longer than the series limit, in agreement with LYOT's observations of polarisation. One may observe therefore  $E_{\lambda c}/E_{Ba_c}$  and then equation (6) yields  $\bar{n}_1/T_e^{3/2}$ ,<sup>17)</sup> which is WURM's method. However, unless the electron temperature is high, or the concentration a good deal higher than assumed, the  $C$  spectrum is relatively weak and a reliable determination of  $T_e$  is not possible on this basis.

Substituting the measured  $\bar{n}_1/T_e^{3/2}$  or  $n_e/T_e^{3/2}$  (6b) into (5), one obtains  $\varepsilon_{\lambda c}/T_e^{3/2}$ , and then (1a)  $E_\lambda = (\varepsilon_\lambda/T_e^{3/2}) L T_e^{3/2}$  yields  $L T_e^{3/2}$ . In other words, if the electron temperature be known, one can determine both the concentrations  $n_1$  or  $n_e$  and the thickness  $L$  of the prominence.

<sup>16)</sup> A. UNSÖLD, Physik der Sternatmosphären, p. 415, 419 (SPRINGER 1938).

<sup>17)</sup> Dividing the observed  $E_{\lambda c}/E_{Ba_c}$  by its value for  $10,000^\circ$  read from the lower dotted curve of Fig. 3, one obtains directly  $\left(\frac{T_e}{10^4}\right)^{3/2} \cdot \frac{10^{10}}{n_1}$ , instead of using (6b).

5. Remark on the continuous spectrum due to the formation of  $H^-$ 

CHANDRASEKHAR and Mrs. BREEN<sup>18</sup>) have computed the absorption coefficient of negative hydrogen  $\alpha_p$ , expressed per neutral hydrogen atom and per unit of electron temperature for various temperatures and wave-lengths. For temperatures up to about 10,000° and wave-lengths near  $\lambda$  3646, forced transitions are negligible, as may be seen by comparing their Tables 5 and 6. For a given electron temperature  $T_e$ , electron pressure  $p_e$  and concentration of neutral hydrogen  $n_0$  the number of recombinations and electron switches for a certain velocity interval, and therefore the emission in a certain wave-length interval, is then the same as for thermal equilibrium at a temperature equal to  $T_e$ . Or also: the emission per unit wave-length and unit solid angle per cm<sup>3</sup> per second  $\epsilon_{\lambda H^-}$  is the same as the absorption for  $T = T_e$ , and therefore given by

$$(9) \quad \epsilon_{\lambda H^-} = B(\lambda, T_e) \cdot \alpha_p(\lambda, T_e) \cdot k T_e n_e n_0$$

where  $B(\lambda, T_e)$  is the intensity of black body radiation, and  $p_e = n_e k T_e$  has been substituted.

From their Table 5 for  $\alpha_p$ , equation (9) and KRAMERS' theory, viz. equation (4), we obtain, for  $\lambda$  3647, by a slight linear extrapolation

$$(10) \quad \left\{ \begin{array}{l} T_e = 5040^\circ, \quad \frac{\epsilon_{3647H^-}}{\epsilon_{Ba_c}} = 2.2 \times 10^{-4} \frac{n_0}{n_1}, \\ T_e = 10,080^\circ, \quad \frac{\epsilon_{3647H^-}}{\epsilon_{Ba_c}} = 5.3 \times 10^{-3} \frac{n_0}{n_1}, \end{array} \right.$$

as a general theoretical result, holding therefore for the chromosphere as well as for prominences.

An actual determination of  $n_0$  has not been devised as yet. However, WURM,<sup>19</sup>) by comparing the ionisation of  $Sr^+$  into  $Sr^{++}$  with the ionisation of  $H$  into  $H^+$ , and assuming a plausible abundance ratio of  $Sr$  to  $H$  estimates for prominences  $n_0/n_1$  between 1 and 0.1, so that the ratio (10) of  $H^-$  to  $Ba_c$  spectrum would be less than  $1/200$  for an electron temperature of 10,000° or lower. An estimate for the chromosphere has not been carried out, but assuming the same or a smaller  $n_0/(n_1 n_e)$  and a ten times larger  $n_e$ , the ratio of the two spectra would be smaller than  $1/20$ .

Pending further evidence, it might be well to keep the possibility of the  $H^-$  spectrum in the chromosphere in mind. If it be present, this would make the determined  $T_e$  still lower.

The writer wishes to express his gratitude to Professor H. H. PLASKETT for clarifying discussions, in particular regarding the STARK effect as means of determining the chromospheric concentration.

<sup>18</sup>) S. CHANDRASEKHAR and FRANCES HERMAN BREEN, Ap. J. 104, 430 (1946).

<sup>19</sup>) K. WURM, loc. cit.